

# RPC 2020



## Virtual Research Presentation Conference

Optimization of atomic clock design as pertains to the impact of LO noise and environmental disturbances

**Principal Investigator: Daphna Enzer (335E)**

**Co-Is: Andrey Matsko (335E), David Murphy (335A), Eric Burt (335E)**

**Program: Spontaneous Concept**

Assigned Presentation # RPC-184



**Jet Propulsion Laboratory**  
California Institute of Technology

# Tutorial Introduction

## Abstract

We have improved an atomic-clock model to calculate **a new noise metric to characterize clock-environment interactions.**

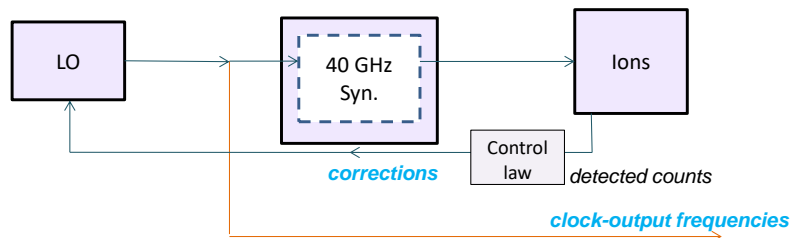
Atomic clocks operate by comparing a local oscillator (LO) to an atomic frequency standard at regular intervals and applying *corrections* at each iteration. We report on these *corrections* and how their noise profile relates to *output* noise.

- Noise/Instability on timescale  $\tau$ : characterized by Allan deviation (ADEV)  $\sigma_y(\tau)$  [for any  $y(t)$  frequency series]

$$\sigma_y^2(\tau) = E[(\langle y(t - \tau) \rangle - \langle y(t) \rangle)^2]/2$$

( $E[\ ]$  and  $\langle \rangle$  both denote simple averages but over different samples and sample sizes.)

- Traditional clock performance metric: ADEV of *output frequency*



noise-floor:

$$\sigma_{y_{out}}(\tau) = \frac{1}{\pi SNR Q} \sqrt{T_c/\tau}$$

- In contrast, will introduce the ADEV of clock *corrections*. Either ADEV can be degraded above noise-floor due to imperfect LOs or environmental disturbances. In this task we specified the relationship between the two ADEVs, **to help identify the source of such disturbances.**



## Problem Description

### a) Context:

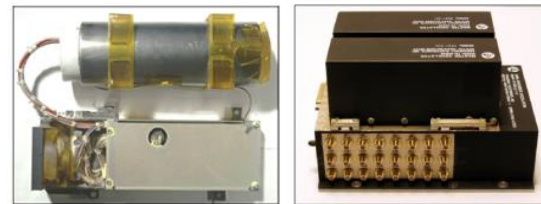
- Atomic clocks more often operating in **space or remote test environments**.
- More **environmental disturbances** (e.g. temperature, magnetic, radiation).
- More need to understand **LO sensitivities** and how **LO variation impacts clock output**.
- Typical state-of-the-art LO used is **Ultra-Stable Oscillator (USO)**.
- **Would like to develop a compact Photonic LO (PLO) for the mercury ion clock**; needed to find out the performance capability.

### b) Comparison to state-of-the-art and Relevance to NASA and JPL:

- Part 1: New *Corrections-ADEV* diagnostic
  - Can allow for efficiently **proving/disproving LO as source** of clock output disturbances.
  - Can allow for efficiently **characterizing LO** response to environmental disturbances.
  - These help illuminate space-clock sensitivities and **design better space-clocks** for the future.
  - Already, this is a useful **tool for the DSAC mission** (Deep Space Atomic Clock). 1) Other techniques to diagnose the source of disturbances involve averaging data series and looking for correlations with other channels; not always conclusive. 2) Understanding USO in space environment also crucial for future missions.

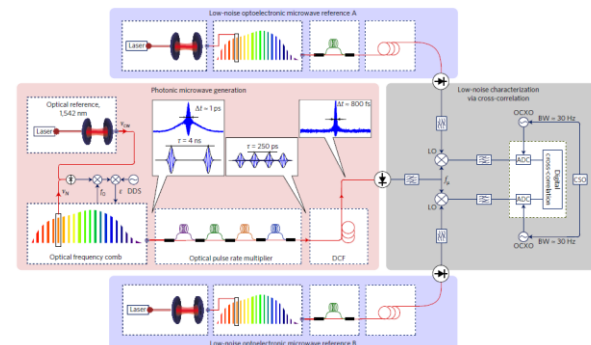
Part 2: Our **Photonic LO modeling** could enable better clocks for the future. In particular, it will allow us to **propose an experimental Task**.

### Quartz Space USO Example:



Bloch, M., Mancini, O., McClelland, T., "What We Don't Know About Quartz Clocks in Space," *Proceedings of the 41st Annual Precise Time and Time Interval Systems and Applications Meeting*, Santa Ana Pueblo, New Mexico, November 2009, pp. 457-472.

### PLO Example:



LETTERS

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nature  
photonics

### Photonic microwave signals with zeptosecond-level absolute timing noise

Xiaopeng Xie<sup>1</sup>, Romain Bouchand<sup>1</sup>, Daniele Nicolodi<sup>1</sup>, Michele Giunta<sup>2,3</sup>, Wolfgang Hänse<sup>1</sup>, Matthias Lezius<sup>7</sup>, Abhay Joshi<sup>4</sup>, Shubhashish Datta<sup>4</sup>, Christophe Alexandre<sup>8</sup>, Michel Lours<sup>9</sup>, Pierre-Alain Tremblin<sup>6</sup>, Giorgio Santarelli<sup>6</sup>, Ronald Holzwarth<sup>2,3</sup> and Yann Le Coq<sup>1\*</sup>



# Methodology

## Part 1: New Corrections-ADEV Diagnostic

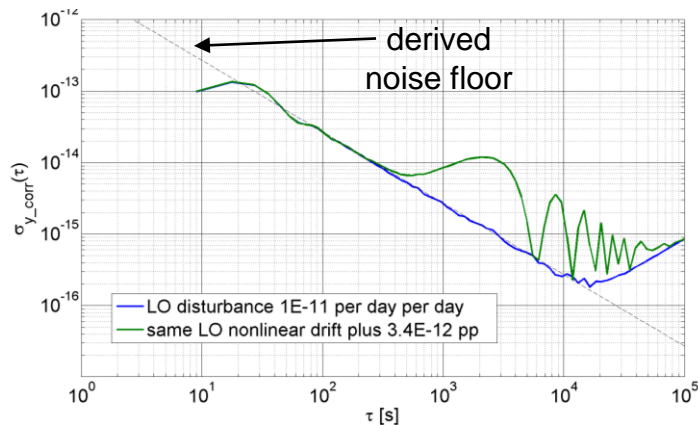
- Derived **noise-floor** of new corrections-ADEV. Confirmed with clock model.
- Derived impact of **LO sinusoidal and/or drift disturbance**. Confirmed with clock model.
- Compared to** disturbing the **atomic/ion reference frequency** rather than the LO.
- Used new diagnostic to **analyze laboratory clock data**. Uncovered unusual noise floor behavior in some configurations that could lead to better understanding of our mercury lamp and detection system if investigated further.

## Part 2: PLO Modeling

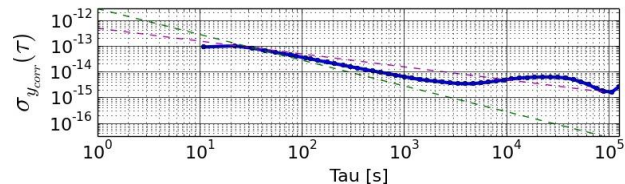
- Researched parameters to model (for both the PLO and for the mercury ion clock).
- Modeled performances.



Example model results for corrections-ADEV: noise floor and impact of LO disturbances



Example experimental results for corrections-ADEV



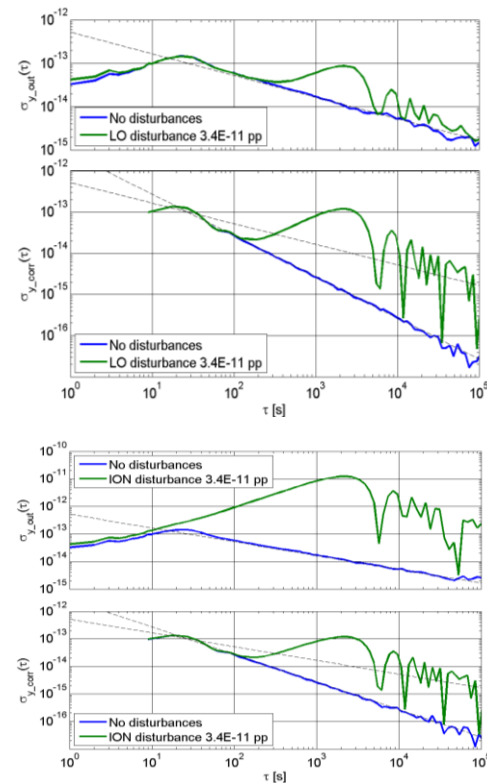
## Results

### Part 1: Corrections-ADEV Diagnostic

- Led to paper, to submit to *IEEE Transactions on Ultrasonics, Ferroelectrics, and Frequency Control (TUFFC)*

- Accomplishments versus goals: **Corrections versus Output ADEV Comparison led to useful diagnostic for a space clock.**
  - A peak/drift due to LO appears roughly the same on the two ADEVs, whereas if due ion-resonance-frequency changes, it appears much bigger on the output-ADEV.
  - Satisfies goal of developing a better data processing algorithm, to figure out clock-stability limitations and to improve the clock performance.
- Significance: **Will help interpret space clock performance and limitations. Will also help characterize LO response to environmental disturbances. Both will aid in improving future space clock design and performance.**
- Next steps:
  - Publish this work. Start using diagnostic for clock analysis.
  - Further study of unusual mercury lamp behavior.

### LO vs Ion Frequency Disturbances (to both ADEVs)



## Results

### Part 2: PLO Modeling

a) Accomplishments versus goals: **Modeled best performing JPL mercury clock with PLO vs USO to predict factor of 5-10 improvement, which was the goal. (green vs. blue curve, top plot)**

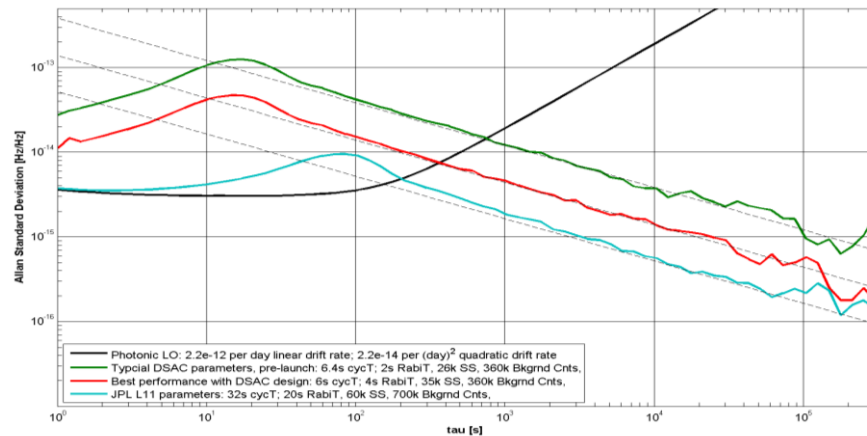
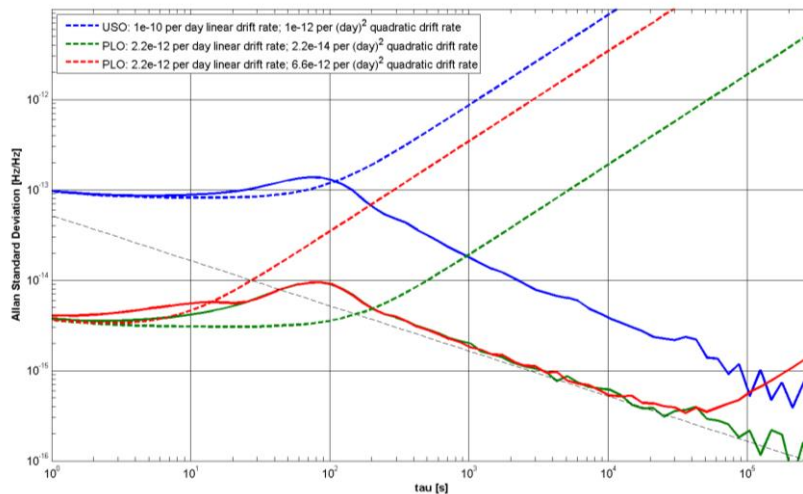
a) Showed this PLO improvement relies on high SNR clock, at least for long term performance. (Lower plot shows degraded performance for lower SNR clocks. Caveat: loop parameters could be adjusted to give PLO level performance at short time scales.)

b) Significance:

a) Indicates potential usefulness of photonic local oscillators in mercury ion clocks.

c) Next Steps:

a) Attract funding for experimental testing of this idea as well as for the development of space-qualified clocks containing a photonic local oscillator.



## Publications and References

- Daphna Enzer, David Murphy, Eric Burt, “Allan Deviation of Atomic Clock Frequency-Corrections: A New Diagnostic Tool for Characterizing Clock Disturbances,” *IEEE Transactions on Ultrasonics, Ferroelectrics, and Frequency Control (TUFFC)*, 2020. **In preparation**
- Daphna Enzer, David Murphy, Eric Burt, “Allan Deviation of Atomic Clock Frequency-Corrections: A New Tool for Characterizing Clock Disturbances,” *Precise Time and Time Interval Systems and Applications (PTTI)*, San Diego, CA, 2021. **In preparation**
- Andrey Matsko, Daphna Enzer, Eric Burt, Robert Tjoelker “On Impact of Local-Oscillator Phase-Noise on Atomic Clock Performance,” *Precise Time and Time Interval Systems and Applications (PTTI)*, San Diego, CA, 2021. **In preparation**